

# Uncertainty Modeling for Data from Remote Sensing Images Using Copula Based Indicator Approaches

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## Introduction

- Indicator geostatistic approaches have been used to estimate uncertainty models of environmental information as soil and hydrological properties, atmospheric and weather data, elevations, ...
- This work explores these approaches, that depend on the variogram (semivariogram) evaluations, to model the uncertainties of remote sensing image information.
- Bivariate copulas can be used to estimate variances (semivariances), instead of traditional mean variograms, to model the spatial variability of the considered attribute.
- Unlike traditional semivariograms, copula variograms represent dependence over the whole range of quantiles, including the extremes, and are not sensitive to outliers.

## Objective

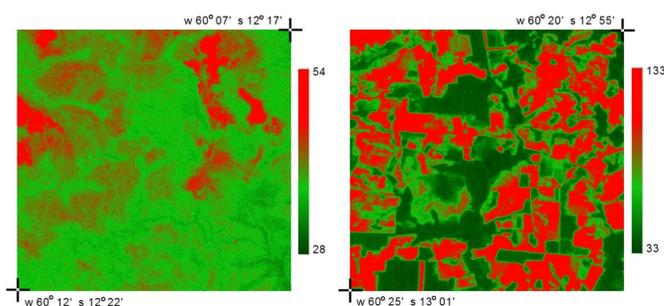
- Assess uncertainty models for remote sensing images using indicator approaches, kriging estimations and sequential simulations, based on bivariate copulas.

## Considerations

- Indicator variograms are determined considering empirical bivariate copulas for various spatial distances values.
- The uncertainty models are used to perform spatial interpolation at image locations with missed or mislead information caused by clouds and shadows, for example.
- A case study is presented with China-Brazil Earth Remote Satellite (CBERS) images from the Brazilian Amazon forest considering forest and partially deforested regions.

## Case Study

- Two small regions of a CCD CBERS Band3 image, patches of 171/114 path/row scene from the state of Rondônia, Brazil, acquired in September, 01, 2008.
- The image of region 1 (left) represents natural forest area while the image of region 2 (right) represents a partially deforested area.
- Each image has 20 m x 20 m spatial resolutions, 8 bits radiometric resolution and size of 500 rows x 500 columns.



## Methodology

- Define the image sensor and bands to be considered (CBERS - Band3);
- Create a random sample set, of 10000 points, from the images, to be used for representing the spatial radiometric variation;
- Determine a set of cutoff values ( $\beta$ ) to represent the uncertainty model;
- Calculate empirical bivariate copulas for the defined cutoffs and for different distance values  $h$ ;
- Considering the cutoffs and the distance values, evaluate empirical indicator semivariograms using empirical bivariate copulas by the following relation, (Bardossy, 2006):

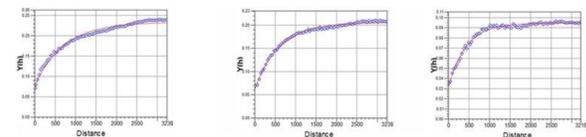
$$\gamma_{\beta}(h) = F_z(\beta) - C_S(h, F_z(\beta), F_z(\beta))$$

- Fit the empirical indicator semivariograms with theoretical models;
- Run indicator kriging estimations or sequential simulations on image locations or areas with missed or mislead information.

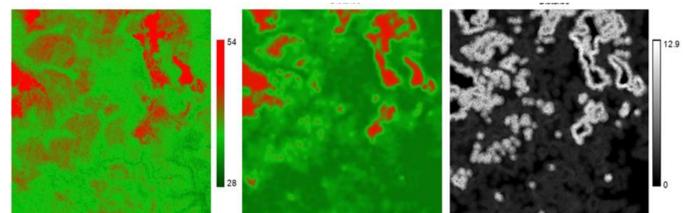
## Results / Analysis

### Semivariograms and Estimations in Region 1

- It was considered 3 cutoffs (33, 34 and 35) closer to the quartile values to evaluate the copula based semivariograms.

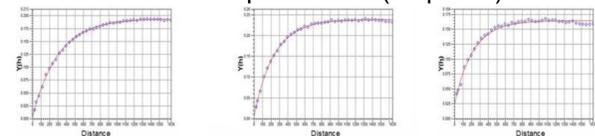


- The nugget effect were high mainly due to the low variability of the band 3 data in the region. Exponential models adjusted the empirical semivariograms with low Akaike Criterion values.
- The samples of the original image (left) and the semivariograms above yielded expected visual results for the kriging estimates (middle) along with their standard deviation uncertainties (right).

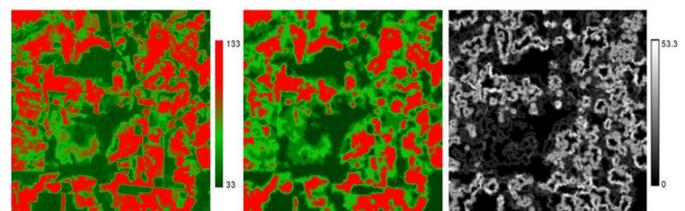


### Semivariograms and Estimations in Region 2

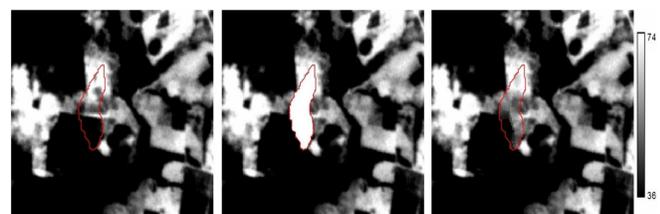
- It was considered 3 cutoffs (39, 50 and 60) closer to the quartile values to evaluate the copula based (empirical) semivariograms.



- Exponential models adjusted the empirical semivariograms with low Akaike Information Criterion (AIC) values.
- The samples of the original image (left) and the semivariograms above yielded expected visual results for the kriging estimates (middle) along with their standard deviation uncertainties (right).



### Application for missing/mislead values (an example)



## Conclusions

- This work showed that is feasible to model uncertainties for remote sensing image data using copula based semivariograms along with indicator approaches, including sequential simulations.
- The copula based semivariograms of this work were shown to be representative of the variability of the image data.
- Qualitative visual analysis showed high similarity between the original and the estimated information. Uncertainty maps can be used to qualify the estimations.
- The random sample set was used to generate the semivariograms while the estimates was done directly from image information closer to the area of interest.
- Future researches should be done to get more qualitative and quantitative results in the presented methodology and making use of other source data set.

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