

Correlation between speed of the stepped leader and peak current of the return stroke of lightning flashes

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Abstract

This study analyzes the two-dimensional speed profiles of 107 stepped leaders and 93 dart leaders recorded by high-speed cameras in Utah (USA), together with data from lightning location system (NLDN). The results show that the stepped leader speed right before the ground contact (final speed) has a very strong correlation ($R = 0.85$) with the peak current of the initiated return stroke. It also shows that the correlation between the average speed and the peak current of the return stroke is strong ($R = 0.73$). The same analysis for dart leaders did not show any significant correlation with the peak current of the prospective return stroke ($R = 0.41$ to average speed and $R = 0.29$ to final speed). This paper discusses why stepped leaders exhibit a significant correlation, while dart leaders do not. In addition, why final speed is better correlated with peak current than average speed.

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Key Points:

- Analysis of the correlation between the speed of the stepped leaders and the following return stroke.
- A significant correlation was found between the final speed of the stepped leader and the stroke peak current.
- No significant correlation was found between dart leaders speed and stroke peak current.

Abstract

This study analyzes the two-dimensional speed profiles of 107 stepped leaders and 93 dart leaders recorded by high-speed cameras in Utah (USA), together with data from lightning location system (NLDN). The results show that the stepped leader speed right before the ground contact (final speed) has a very strong correlation ($R = 0.85$) with the peak current of the initiated return stroke. It also shows that the correlation between the average speed and the peak current of the return stroke is strong ($R = 0.73$). The same analysis for dart leaders did not show any significant correlation with the peak current of the prospective return stroke ($R = 0.41$ to average speed and $R = 0.29$ to final speed). This paper discusses why stepped leaders exhibit a significant correlation, while dart leaders do not. In addition, why final speed is better correlated with peak current than average speed.

Plain Language Summary

Stepped leaders and dart leaders propagate differently, exhibiting characteristic speeds during their development. On average, the speed of dart leaders is 100 times higher than that of stepped leaders. The speeds of darts and stepped leaders may vary during their propagation (increase or decrease). Some leaders can present speed differences of up to 10 times compared to other strokes. The present work shows that differences in the speeds of the stepped leaders are associated with differences in the intensity of the discharges (peak current). This work shows that lightning flashes with high peak currents tend to have higher final speeds, and lightning flashes with lower peak currents have lower final speeds.

38 **1 Introduction**

39 Negative cloud-to-ground lightning flashes originate from bidirectional and bipolar leaders in
40 thunderclouds (Mazur, 1989). The positive end of these bidirectional and bipolar leaders
41 propagates within the cloud and the negative end propagates towards the ground. The development
42 of the negative downward leader occurs in a stepped manner. The length of the steps can vary from
43 3 to 200 m in intervals between 0.2 and 100 μ s. The observed average speed of the stepped leader
44 varies between 0.8 and 39×10^5 m/s (Beasley et al., 1983; Berger, 1967; Campos et al., 2014; Chen
45 et al., 1999; Krider, 1974; Lu et al., 2008; Mazur et al., 1995; Orville & Idone, 1982; Proctor et
46 al., 1988; Schonland et al., 1935; Thomson et al., 1985).

47
48 When the stepped leader touches the ground, the first return stroke occurs. Then, after the decay
49 of the lightning channel, subsequent return strokes may occur. A subsequent return stroke is
50 originated by dart leaders or by dart-stepped leaders. Dart leaders re-ionize a previously ionized
51 channel, developing with a higher average speed, which varies between 1 and 50×10^6 m/s (Jensen
52 et al., 2021; Jordan et al., 1992; Loeb, 1966; Schonland et al., 1935; Shao et al., 1995; Stock et al.,
53 2014). Dart-stepped leaders exhibit two behaviors: fast development as a dart leader, since they
54 develop through a previously ionized medium, and stepped development, as it propagates through
55 a non-ionized medium (Petersen & Beasley, 2013; Wang et al., 2016; Ding et al., 2024).

56
57 The amount of charge at the tip of the leader is believed to be correlated with propagation speed
58 of the leader as well as with the intensity of the prospective return stroke (Proctor et al., 1988).
59 Campos et. al (2014) compared the average speed of stepped leaders and dart leaders with their
60 respective peak currents. However, in both analyses there was no correlation. The present work
61 shows that the final speed of the stepped leaders has a significant correlation with the peak current
62 of the return stroke and offers an explanation why Campos et. al (2014) did not obtain a correlation
63 in their results.

64 **2 Instruments**

65 **2.1 Lightning location systems (LLS)**

66 Data from National Lightning Detection Network (NLDN) was used to identify the polarity, peak
67 current and location of the analyzed lightning flashes. For more network information, see Biagi et
68 al. (2007), Cummins & Murphy (2009) and Abarca et al. (2010). LLSs measure the radiated
69 electromagnetic fields using multiple sensors at different locations. The time difference of arrival
70 of these fields then allows for localization and the amplitude of the fields allows peak current
71 inference. This is done by applying a simple “transmission line” model relating the measured
72 electromagnetic field amplitude to the peak current along with the distance from the sensor to the
73 termination location and the speed of light, see Cummins & Murphy (2009). This has been shown
74 (mostly through rocket triggered lightning studies) to estimate the peak current well (errors within
75 10% to 15%) for negative subsequent strokes, although there is still little experimental data for
76 first return strokes and positive strokes (Rakov, 2005).

77 **2.2 High-speed cameras**

78 In this work, a Phantom v2012 high-speed camera equipped with a 20 mm lens was used. The
79 camera was installed west of Hinckley, Utah, in Millard County (USA). This is a desert region
80 with flat relief, making it easier to observe the entire propagation of the leader, towards the ground.

81 The lightning flashes were filmed at an acquisition rate of 40,000 fps, with a period of 25 μ s, and
 82 image spatial resolution of 1,280 x 448 pixels, same settings used by Abbasi et al. (2023).
 83 Calculations of the two-dimensional (2-D) speed of the leaders were obtained with the analysis of
 84 the high-speed camera videos in conjunction with the LLS data. The method used for the
 85 calculations was the same as that used by Campos et al. (2014), Saba et al. (2017), Saba et al.
 86 (2022) and Saba et al. (2023).

87 **3 Data**

88 The data was obtained during the summers of 2021, 2022 and 2023. A total of 281 return strokes
 89 of 126 lightning flashes were analyzed: 126 negative first return strokes and 155 negative
 90 subsequent return strokes. The dart-stepped leaders were not included in the analysis, as they hold
 91 two types of propagation: stepped and continuous.

92
 93 Excluding all dart-stepped leaders and the leaders whose distances were not possible to determine
 94 as the resulting return strokes were not detected, a total of 107 stepped leaders and 93 dart leaders
 95 had their 2-D speed profile analyzed. The return strokes from stepped leaders had an average peak
 96 current of -35 kA and occurred at an average distance of 18 km (with minimum distance of 3 km
 97 and maximum distance of 46 km) from the high-speed camera. Return strokes from dart leaders
 98 occurred at an average distance of 22 km (with minimum distance of 8 km and maximum distance
 99 of 44 km), with an average peak current of -17 kA (see table 1).

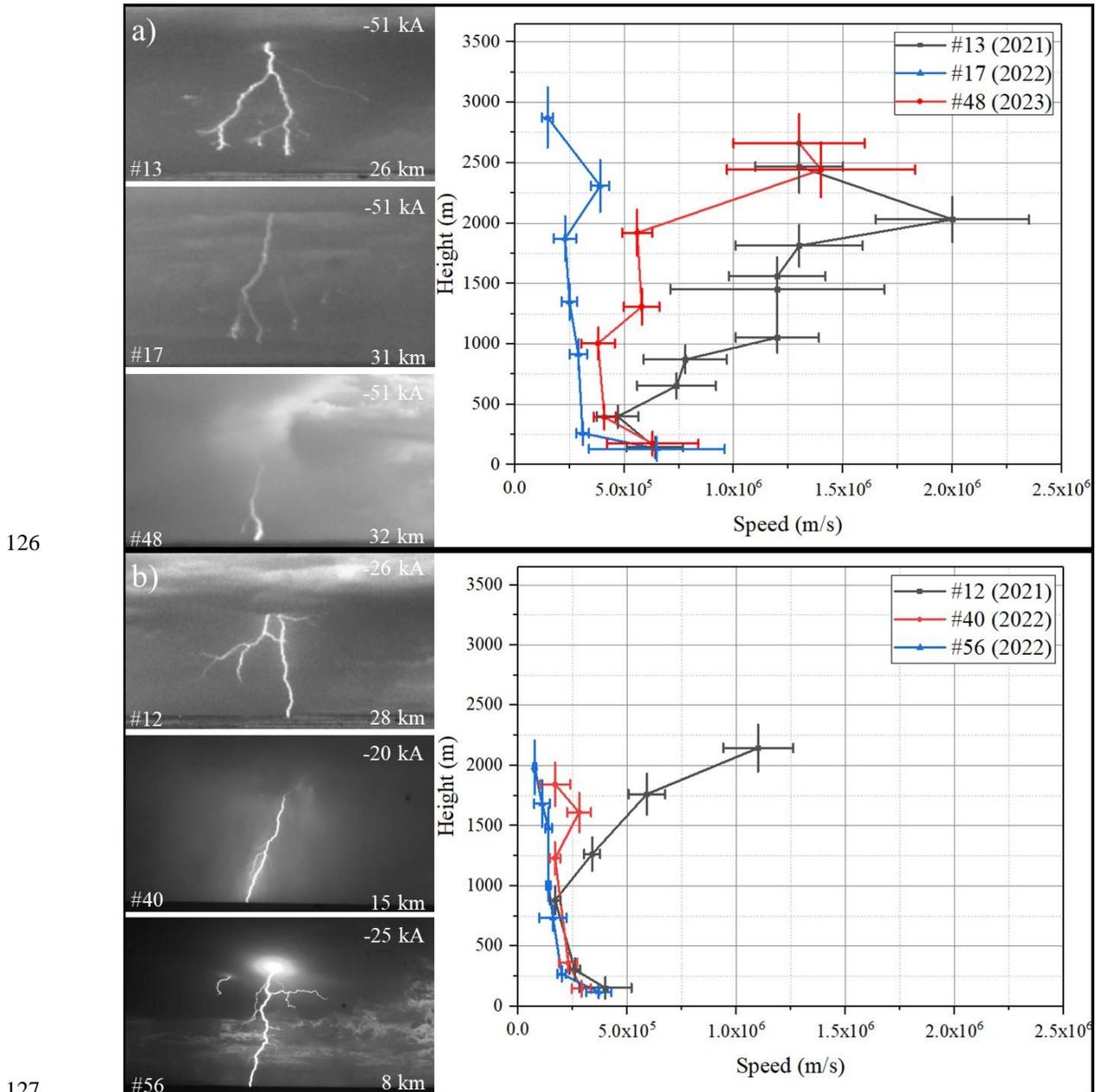
100 **4 Analysis**

101 **4.1 Stepped leader**

102 Figure 1a shows the 2-D speed profiles of three stepped leaders from three different lightning
 103 flashes. It was possible to trace the speed profiles of the leaders from near the base of the cloud
 104 down to the ground. The three return strokes in Figure 1a have the same peak current (-51 kA).
 105 The lightning flashes were numbered in a sequence according to the filming time and year, in the
 106 format “#nn (yyyy)”. They started with different speeds but during the development towards the
 107 ground, the final speeds converged to very close values. The final speed was measured using two
 108 leader tip locations from frames close to the ground, with the lowest height (final height H_F) located
 109 between 50 and 200 m and the second lowest height (H_{F-1}) located between 200 and 450 m above
 110 the ground. See the Figure S1 provided in the supplementary information and ‘data.xlsx’ available
 111 in open research (the videos of these three stepped leaders in .cine format are also available at open
 112 research). The final speeds for these cases were 6.4 ± 1.3 , 6.5 ± 3.1 and $6.3 \pm 2.1 \times 10^5$ m/s for H_F
 113 of 145 ± 52 , 131 ± 62 , and 175 ± 63 m. These stepped leaders occurred 26, 31, and 32 km away
 114 from the high-speed camera, respectively. Measurement errors were calculated, where LLS errors
 115 ($\delta_{LLS} = \pm 500$ m, see Cummins et al.; 1998), camera tilt errors ($\delta_\theta = \pm 0.017$ rad) and pixel location
 116 in high-speed camera videos ($\delta_{px} = \pm 1$ px) were used.

117
 118 Figure 1b shows the 2-D speed profiles of another three stepped leaders with return stroke current
 119 peaks of -26, -20, and -25 kA (videos in .cine format of these three stepped leaders are also
 120 available in open research). The values are approximately half of those in the previous cases, but
 121 also relatively close to each other. These leaders also started with different speeds and the final
 122 speed converged to close values. The final speed for these cases were 4.0 ± 1.2 , 2.9 ± 0.44 , and

123 $3.7 \pm 0.58 \times 10^5$ m/s the H_F were 153 ± 55 , 148 ± 32 , and 119 ± 19 m to the ground. The lightning
 124 flashes occurred 28, 15, and 8 km away from the high-speed camera, respectively.
 125



126

127

128 **Figure 1.** The 2D speeds of the stepped leaders vs height. On the left part of figures a) and b), the
 129 images of the stepped leaders are shown, together with peak current and distance from camera. On
 130 the right of the figures, the 2-D speed profiles of the stepped leaders as a function of height are
 131 displayed. The horizontal and vertical bars show the values of the speed and height errors.

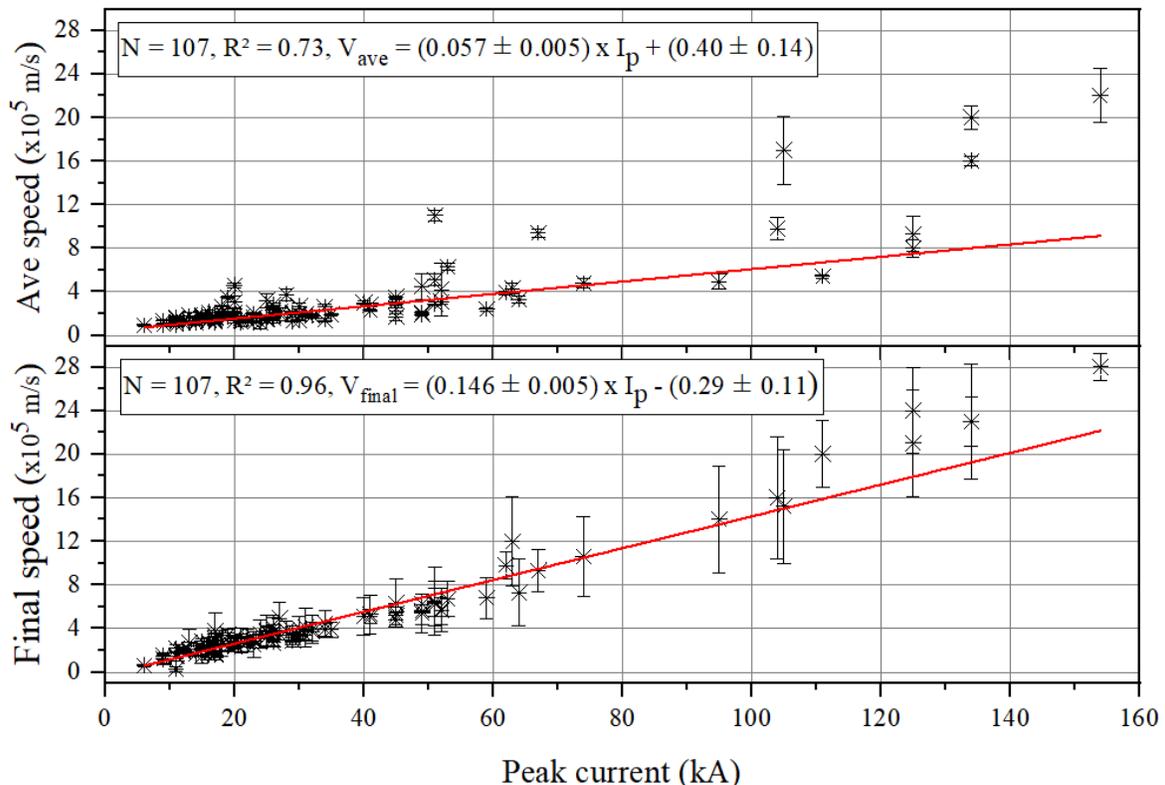
132

133 Figure 1 indicates a possible correlation between the final speed of stepped leaders and the peak
 134 current of the return stroke. It also shows that the propagation speeds of the stepped leaders vary
 135 largely during the propagation thus making the average speed of the stepped leaders not well
 136 correlated with the peak current.

137

138 In order to better investigate the relation between leader speed and prospective return stroke peak
 139 current, Figure 2 shows the average and final speeds of the 107 stepped leaders plotted against the
 140 corresponding prospective return stroke peak current. The average speeds of these lightning flashes
 141 were calculated from a linear regression applied to a scatter plot of the distance propagated by the
 142 leader as a function of time. The angular coefficients of the linear fitting show the values of the
 143 average speeds. Statistics on return stroke peak current and speed values are shown in Table 1.

144



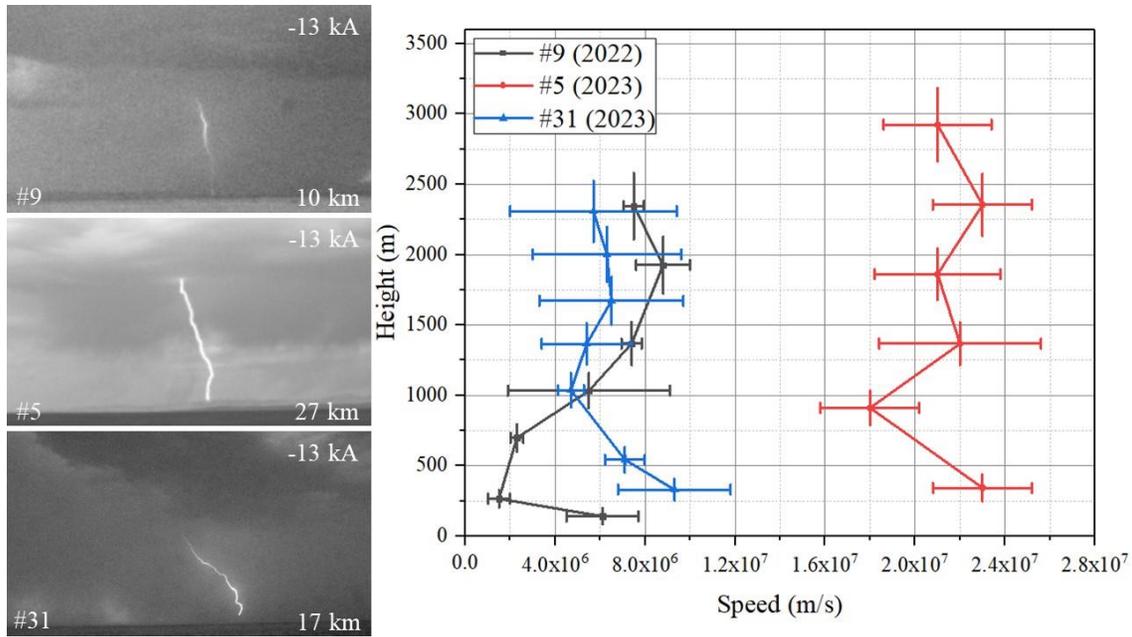
145

146 **Figure 2.** The image shows the average and final speed of the stepped leaders as a function of
 147 prospective return stroke peak current. R^2 represents the coefficient of determination and N
 148 indicates the number of analyzed stepped leaders. In the graphs, the negative sign of the current
 149 peaks are disregarded for better visualization.

150 4.2 Dart leaders

151 Figure 3 shows the 2-D speed profiles of three dart leaders (2nd return stroke of lightning flash #9,
 152 10th return stroke of lightning flash #5 and 8th return stroke of lightning flash #31), all with the
 153 same prospective return stroke peak current (-13 kA). The dart leaders also started with variable
 154 speeds but showed different behavior than stepped leaders regarding the final speed. The final
 155 speed of the dart leaders did not converge to close values, being 6.1 ± 1.6 , 23 ± 2.2 , and
 156 $9.3 \pm 2.5 \times 10^6$ m/s in this case for heights of 140 ± 23 , 342 ± 59 , and 330 ± 42 . The lightning
 157 flashes occurred 10, 27, and 17 km away from the high-speed camera, respectively.

158



159
 160 **Figure 3.** On the left, the video images of the three dart leaders right before the occurrence of the
 161 return stroke are shown. Their estimated peak currents are the same (-13 kA). On the right, height
 162 profiles of the speeds are shown. The horizontal and vertical bars show the values of the speed and
 163 height errors.

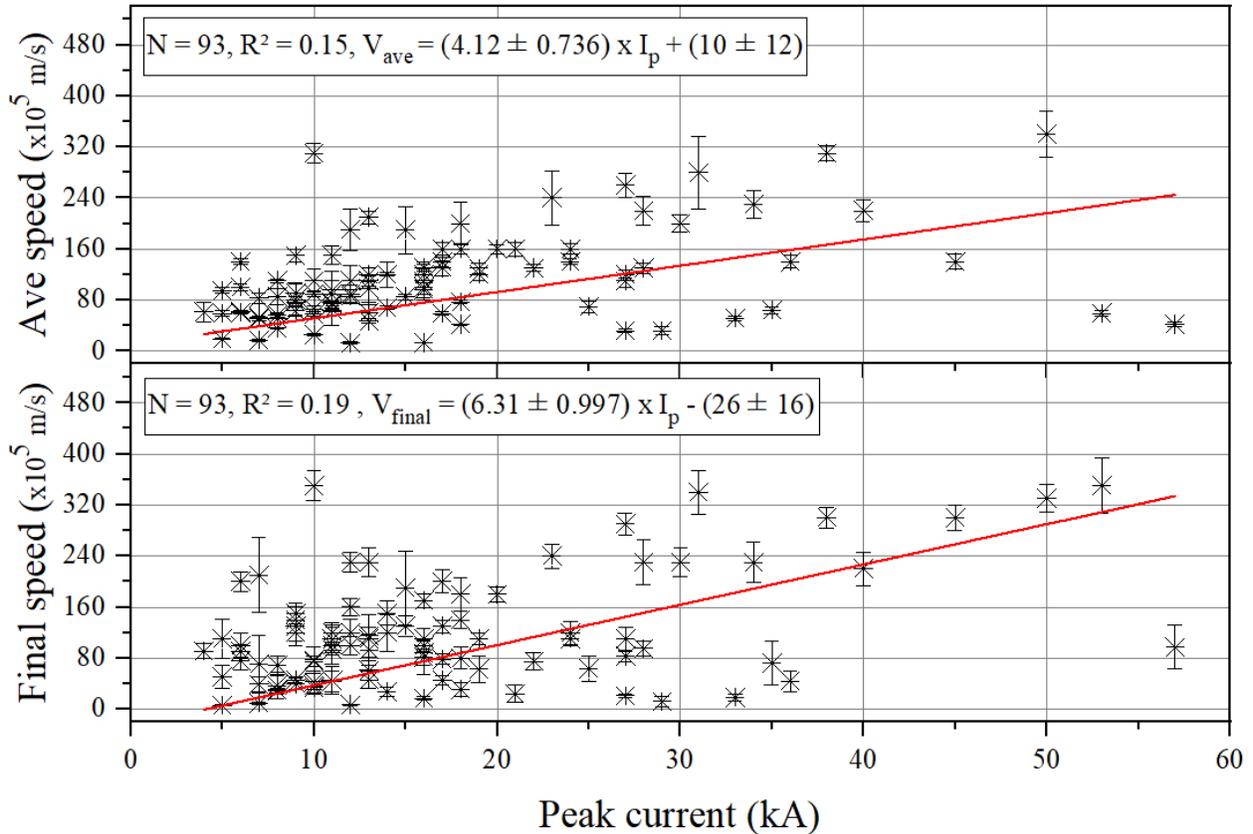
164
 165 In this case, the final speeds have no significant correlation with the peak current. In order to better
 166 investigate the relation between the dart leader speed and prospective return stroke peak current,
 167 the average and final speeds of 93 dart leaders were analyzed (Figure 4). It was only possible to
 168 obtain 39 cases in the same height range of that considered for stepped leaders ($50 \text{ m} \leq H_F \leq 200$
 169 m and $200 \text{ m} \leq H_{F-1} \leq 450 \text{ m}$), as the speed of dart leaders is higher, some cases having their final
 170 steps at a height greater than 300 m. The remaining cases (54 cases), the speed of the dart leaders
 171 were calculated with one frame difference, i.e. a fixed difference of $25 \mu\text{s}$. For the dart leaders, the
 172 heights varied from $50 \text{ m} \leq H_F \leq 760 \text{ m}$ and $200 \text{ m} \leq H_{F-1} \leq 1440 \text{ m}$. See Figure S2 of the
 173 supplementary information and ‘data.xlsx’ available in open research (the videos of these three
 174 dart leaders in .cine format are also available at open research). Statistics on return stroke peak
 175 current and speed values are shown in Table 1.

176

	Ip (kA)		Average Speed ($\times 10^5 \text{ m/s}$)		Final Speed ($\times 10^5 \text{ m/s}$)		
	AM	Min.	Max.	Min.	Max.	Min.	Max.
Stepped leader (N = 107)	-33	-6	-154	0.87	22	0.28	28
Dart leader (N = 93)	-17	-4	-57	13	340	6.2	350

177 **Table 1.** Return stroke peak current and average and final speed values for stepped and dart leaders.
 178 N is the number of stepped and dart leaders analyzed.

179



180

181 **Figure 4.** Average and final speed of the darts leaders as a function of the peak current.
 182 R^2 represents the coefficient of determination and N indicates the number of stepped leaders
 183 analyzed. In the graphs, the negative sign of the current peaks are disregarded for better
 184 visualization.

185 5 Discussion and conclusion

186 Considering that the speed of leaders is expected to be faster if the amount of charge at their tips
 187 is higher (Proctor et al., 1988), and that peak current of the following return stroke is higher if the
 188 amount of charge at the bottom part of the leader is higher (Khounate et al., 2021), Campos et al.
 189 (2014) tried to find some correlation between the speed of the leader and the peak current of the
 190 return stroke. However, they showed that the average speed of positive leaders, negative stepped
 191 and dart leaders have apparently no correlation with the peak currents of the return strokes
 192 following these leaders. The present work reviews that study, using new data to examine the
 193 relationship of the final and average speed of stepped and dart leaders with the stroke peak current
 194 initiated by them. The larger sample size and peak current range unveiled a relationship that has
 195 never been observed before.

196

197 The present work shows that there is a correlation between leader speed and the resulting return
 198 stroke peak current for stepped leaders but not for dart leaders. It also shows that the final speed
 199 of the leader has a better correlation with the final return stroke peak current than the average speed
 200 of the leader values measured along their propagation.

201

202 As observed by Campos et al. (2014), the average speed of negative leaders during their downward
203 propagation has a wide variation. This could be related to atmospheric conditions and to the
204 number of branches formed along their propagation. Therefore, the correlation ($R = 0.73$) of the
205 average speed of a leader with the peak current is weaker than that of the final speed ($R = 0.85$).
206 Considering that both the peak current and leader speed distributions are not normal, the Spearman
207 correlation coefficient was used. The Spearman correlation coefficients obtained in this research
208 were calculated considering the uncertainties in the speeds. For this, 100,000 Monte Carlo
209 simulations were carried out. The values found represent the average correlation coefficient.

210

211 This work shows that the speed of stepped leaders converges to approximate equal final values
212 when the initiated return strokes have similar peak currents. The significant correlation between
213 the final speed and the following stroke peak current can be understood if one considers that the
214 return stroke current is composed by the flow of charges that are concentrated in the final portion
215 (few hundreds of meters) of the downward leader and not by the charges that populate the whole
216 channel. This is also important considering that LLSs are not well validated for the first return and
217 that, while there are possible errors present in the LLS peak current estimation, this is not relevant
218 as the relationship between final speed and peak current clearly holds here.

219

220 The correlations between dart leader speed and return stroke peak current were moderate and weak.
221 The dart leaders presented a correlation coefficient $R = 0.41$ when the average speed was
222 considered, and $R = 0.29$ when the final speed was used. As they propagate in a previously ionized
223 heated channel, the speed of the dart leaders will depend not only on the charge at their tip (as
224 supposed for stepped leaders) but also on other factors like the presence of continuing current
225 (CC), duration of previous interstroke time intervals, and other characteristics that influence the
226 conductivity of the decaying channel. Therefore, the leader speed is not solely related to the
227 quantity of charge stored at the leader tip, resulting in a moderate (average speed) and weak (final
228 speed) correlation with the peak current.

229

230 The fact that the final speed of negative leaders (for $50 \text{ m} \leq H_F \leq 200 \text{ m}$ and $200 \text{ m} \leq H_{F-1} \leq 450$
231 m) has a very strong correlation with the following return strokes not only shed light on the physics
232 of leader propagation and return strokes but also can be of practical use for models dealing with
233 upward leader from structures (Warner, 2010) and for attachment to transmission lines in general
234 (Rizk, 2010a, 2010b, 2024). It is during the final propagation of the downward leader that the
235 upward leaders are induced, incepted and propagate upwards (Saba et al., 2017, 2022, 2023).

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244 **Open Research**

245 The data analyzed in this work are available at Cruz (2024).

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Supporting Information for

Correlation between final speed of the stepped leader and the return stroke peak current of lightning flashes

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Figures S1 to S2

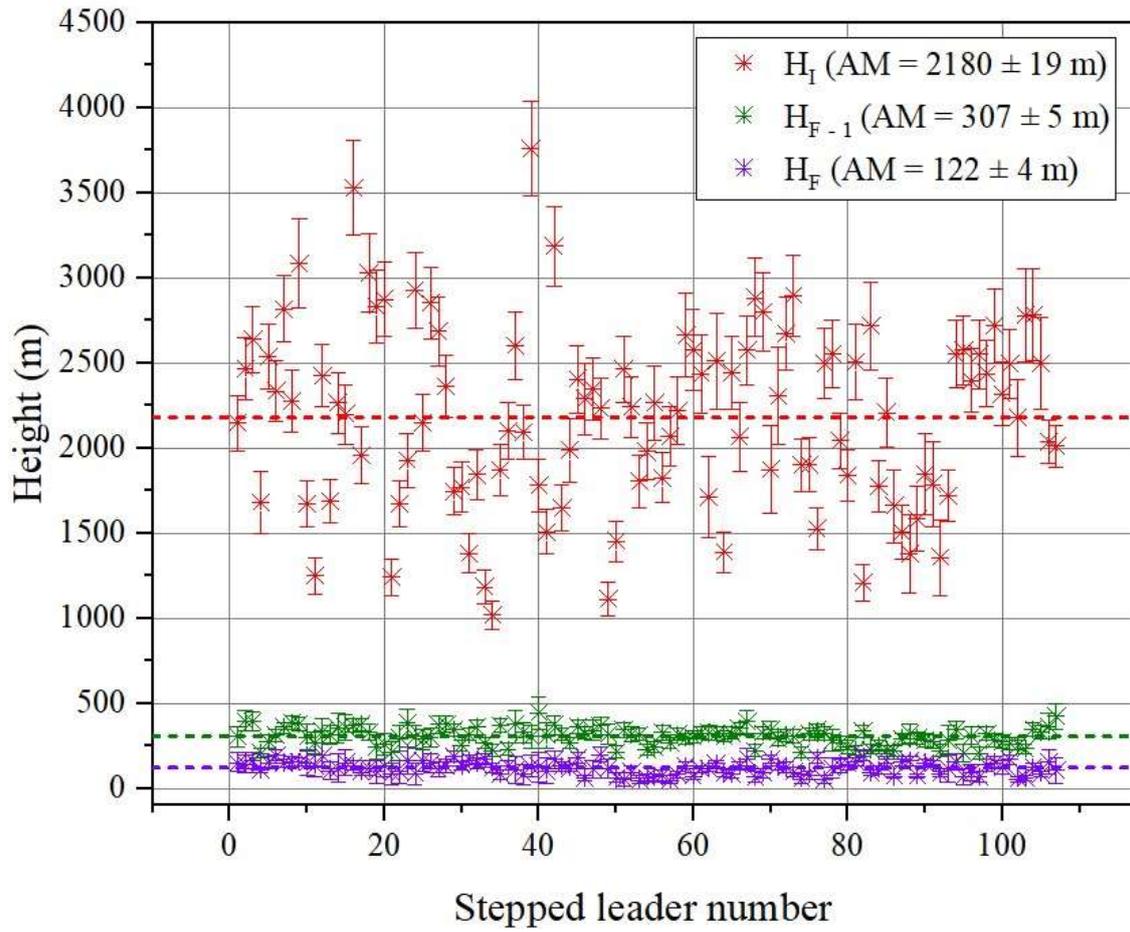


Figure S1. The image shows the distributions of the 107 stepped leaders for height close to the cloud base (initial height – H_I), final height (H_F), and for the penultimate height (H_{F-1}). Vertical bars represent height uncertainties. The red, green, and purple dotted lines display the average height of H_I , H_{F-1} , and H_F .

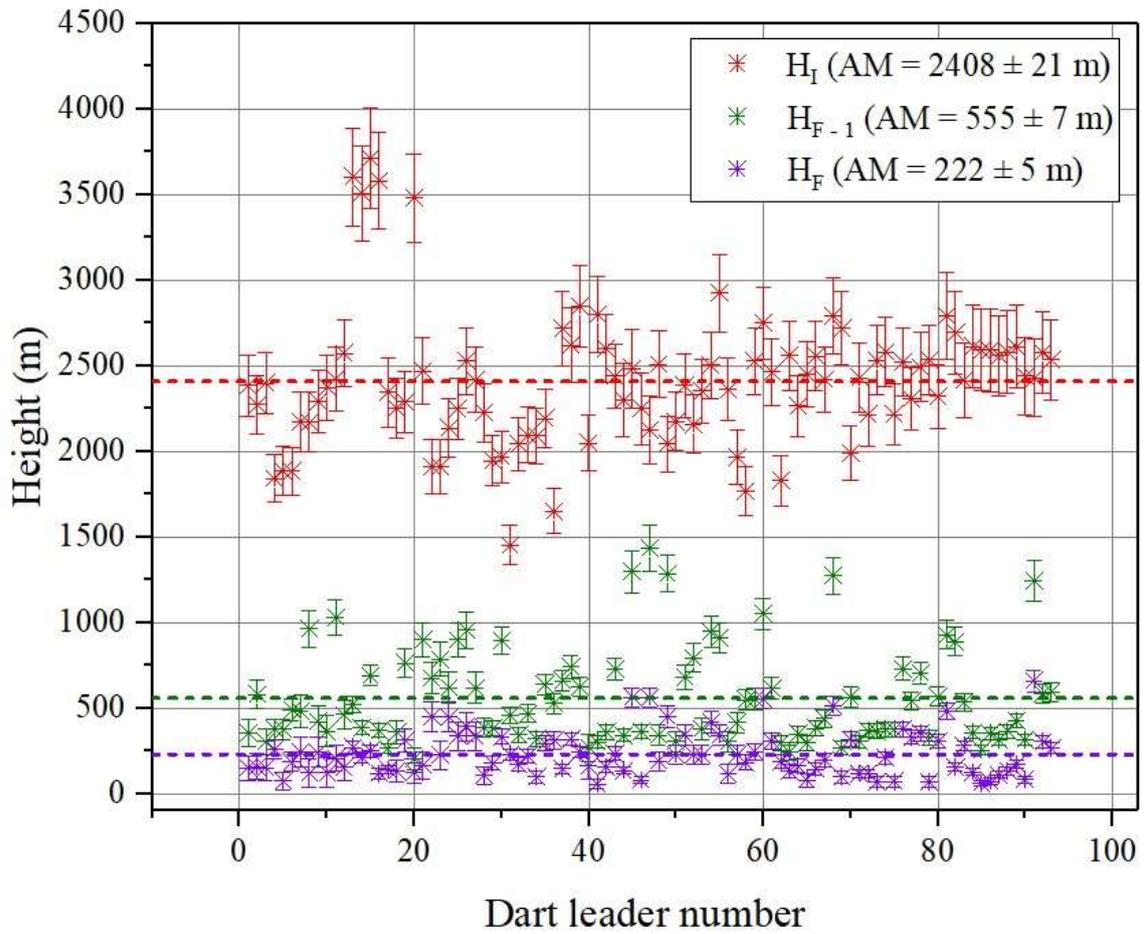


Figure S2. The image shows the distributions of the 93 dart leaders for height close to the cloud base (initial height – H_I), final height (H_F), and for the penultimate height (H_{F-1}). Vertical bars represent height uncertainties. The red, green, and purple dotted lines display the average height of H_I , H_{F-1} , and H_F .